

Assignment 5

- Have a scenario on(one sample t test)
- Identify sample and population
- Extract information
- Write hypotheses
- Interpret results
- Make a conclusion

Example One-Sample T-Test

Scenario: A school claims that the average score of students in a mathematics test is 75. However, a researcher believes that the actual average score might be different from this claimed average. To test this, the researcher collects a random sample of 20 students and records their test scores. The sample mean score is 72.5, and the sample standard deviation is 8. The researcher then performs a one-sample t-test to determine if the mean test score in the sample is significantly different from the population mean of 75. Significance level (α)= 0.05 .

Identifying the Sample and Population:

- Population: *All students in the school*
- Sample: *20 student*

Extracting Information:

- Population mean (μ): *75*
- Sample mean (\bar{x}): *72.5*
- Sample size (n): *20*
- Sample standard deviation (s): *8*
- Significance level (α): *0.05*

Writing Hypotheses:

- Null Hypothesis (H_0): *$\mu = 75$*
- Alternative Hypothesis (H_1): *$\mu \neq 75$*

Performing the t-Test:

$$t = \frac{\bar{x} - \mu}{s/\sqrt{n}} = \frac{72.5 - 75}{8/\sqrt{20}} = -1.397$$

p value $\left\{ \begin{array}{l} \rightarrow \text{two tailed} \\ \rightarrow df = 20 - 1 = 19 \\ \rightarrow \alpha = 0.05 \end{array} \right.$

p-value = 0.179

0.179 > 0.05

p-value > α

Interpreting Results:

We can't reject H_0 because p value is less than α

Conclusion:

at $\alpha = 0.05$ we do not have enough evidence to say that the student average score is different than 75

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Example One-Sample T-Test

Scenario: A coach claims that the average height of basketball players ~~is~~ 6.5 feet. A researcher wants to test whether the average height is different. The researcher collects a sample of 15 players and records their heights. The sample mean height is 6.7 feet, and the sample standard deviation is 0.3 feet. The researcher then performs a one-sample t-test to determine if the mean test score in the sample is significantly different from the population mean. Significance level (α) = 0.05 .

Identifying the Sample and Population:

- Population: *All basket ball players*
- Sample: *15 player*

Extracting Information:

- Population mean (μ): *6.5*
- Sample mean (\bar{x}): *6.7*
- Sample size (n): *15*
- Sample standard deviation (s): *0.3*
- Significance level (α): *0.05*

Writing Hypotheses:

- Null Hypothesis (H_0): *$\mu = 6.5$*
- Alternative Hypothesis (H_1): *$\mu \neq 6.5$*

Performing the t-Test:

$$t = \frac{\bar{x} - \mu}{s/\sqrt{n}} = \frac{6.7 - 6.5}{0.3/\sqrt{15}} = 2.58$$

P-value $\left\{ \begin{array}{l} \rightarrow \text{two tailed} \\ \rightarrow df = 14 \\ \rightarrow \alpha = 0.05 \end{array} \right.$

$$P\text{-value} = 0.022$$

Interpreting Results:

$$P\text{-value} < \alpha$$
$$0.022 < 0.05$$

*we reject H_0 because
P-value is less than*

Conclusion:

at $\alpha = 0.05$ there is enough evidence that the weight of basketball player is different than 6.5

Example One-Sample T-Test

Scenario: A social researcher claims that the average time people spend on social media is **3 hours per day**. However, a new survey suggests that the average might be different. The researcher collects data from a random sample of **30 individuals** and records their daily social media usage. The sample mean usage is **3.5 hours**, and the sample standard deviation is **0.8 hours**.

Identifying the Sample and Population:

- Population: *All people using social media*
- Sample: *30 people using social media*

Extracting Information:

- Population mean (μ): *3*
- Sample mean (\bar{x}): *3.5*
- Sample size (n): *30*
- Sample standard deviation (s): *0.8*
- Significance level (α): *0.05*

Writing Hypotheses:

- Null Hypothesis (H_0): *$\mu = 3$*
- Alternative Hypothesis (H_1): *$\mu \neq 3$*

Performing the t-Test:

$$t = \frac{\bar{x} - \mu}{s/\sqrt{n}} = \frac{3.5 - 3}{0.8/\sqrt{30}} = 3.42$$

p-value $\left\{ \begin{array}{l} \rightarrow \text{two tailed} \\ \rightarrow \alpha = 0.05 \\ \rightarrow df = 29 \end{array} \right.$

$$p\text{-value} = 0.002$$

$$p\text{-value} < \alpha$$

Interpreting Results:

$p < \alpha$ *reject H_0 because p less than α*
 $0.002 < 0.05$

Conclusion:

At $\alpha=0.05$ there is enough evidence to conclude that the average time people spend on social media is different than 3