

$$PV = nRT$$

## Examples Worksheet of Chapter "1"

Use the universal gas constant  $R = 0.0821 \text{ L}\cdot\text{atm} / (\text{K}\cdot\text{mol})$  to solve the following problems:  $\text{K}\cdot\text{mol}$  If pressure is needed in kPa then convert by multiplying by  $101.3 \text{ kPa} / 1 \text{ atm}$  to get  $R = 8.31 \text{ kPa}\cdot\text{L} / (\text{K}\cdot\text{mole})$

1. a 4 moles of a gas at a pressure of 5.6 atm and a volume of 12 liters, what is the temperature?  $T$

$$Pv = nRT$$

$$T = \frac{PV}{nR} = \frac{(5.6 \text{ atm})(12 \text{ L})}{4 \text{ mol} (0.0821 \text{ L}\cdot\frac{\text{atm}}{\text{K}\cdot\text{mol}})} = 204.63 \text{ K}$$

$$PV = nRT$$

$$T = \frac{PV}{nR} = \frac{5.6 \times 12}{4 \times 0.0821} = 204.63 \text{ K}$$

2. An unknown quantity of gas at a pressure of 1.2 atm, a volume of 31 liters, and a temperature of 87 °C, how many moles of?

$$Pv = nRT$$

$$n = \frac{PV}{RT} = \frac{(1.2 \text{ atm})(31 \text{ L})}{(87+273) \text{ K} * (0.0821 \text{ L}\cdot\frac{\text{atm}}{\text{K}\cdot\text{mol}})} = 1.26 \text{ mol}$$

$$T = 87 + 273 = 366$$

$$PV = nRT$$

$$n = \frac{PV}{RT} = \frac{1.2 \times 31}{0.0821 \times 360} = 1.26 \text{ mol}$$

3. A 7.7 moles of gas at a pressure of 0.09 atm and at a temperature of 56 °C, what is the volume of the container that the gas is in?

$$Pv = nRT$$

$$V = \frac{nRT}{P} = \frac{(7.7 \text{ mol})(56+273) \text{ K} * (0.0821 \text{ L}\cdot\frac{\text{atm}}{\text{K}\cdot\text{mol}})}{0.09} = 2310.9 \text{ L}$$

$$V = ?$$

$$PV = nRT$$

$$V = \frac{nRT}{P} = \frac{7.7 \times 0.0821 \times 329}{0.09} = 2310.9 \text{ L}$$

4. A 17 moles of gas at a temperature of 67 °C, and a volume of 88.89 liters, what is the pressure of the gas?

$$Pv = nRT$$

$$P = \frac{nRT}{V} = \frac{(17 \text{ mol})(67+273) \text{ K} * (0.0821 \text{ L}\cdot\frac{\text{atm}}{\text{K}\cdot\text{mol}})}{88.9} = 5.34 \text{ atm} = 540.61 \text{ kPa}$$

$$T = 67 + 273 = 340 \text{ K}$$

$$PV = nRT$$

$$P = \frac{nRT}{V}$$

$$P = \frac{17 \times 0.0821 \times 340}{88.89} = 5.34 \text{ atm}$$

$$536 \times 10^{-3}$$

5. Carbon dioxide gas (1.00 mole) at 373 K occupies 536 mL at 50.0 atmosphere pressure. What is the calculated value of the pressure using:

(i) Ideal gas equation  $PV = nRT$

(ii) Van der Waals equation?

Van der Waals equation

$$\left(P + \frac{a}{V^2}\right)(V - b) = RT$$

[Data - Van der Waals constants for carbon dioxide:

$$a = 3.61 \text{ L}^2 \text{ atm mol}^{-2}; b = 0.0428 \text{ L mol}^{-1}$$

i) Using the Ideal Gas Equation

$$V = 0.536 \text{ L}$$

$$n = 1.00 \text{ mol}$$

$$T = 373 \text{ K}$$

$$PV = nRT$$

$$P = \frac{nRT}{V} = \frac{(1 \text{ mol})(373 \text{ K}) \cdot (0.0821 \frac{\text{L} \cdot \text{atm}}{\text{K} \cdot \text{mol}})}{0.536 \text{ L}} = 57.1 \text{ atm}$$

ii) the Van der Waals equation for real gas behavior:

$$(P + \frac{an^2}{V^2})(V - nb) = nRT$$

$$P + 3.61 \times (1.00/0.536)^2 (0.536 - 1.00 \times 0.0428) = 1.00 \times 0.0821 \times 373$$

$$(P + 12.57)(0.493) = 30.62$$

$$P + 12.57 = 62.12$$

$$P = 49.6 \text{ atm}$$

$$\left(P + \frac{an^2}{V^2}\right)(V - nb) = nRT$$

$$a) \quad PV = nRT \quad P = \frac{nRT}{V}$$

$$P = \frac{1(0.0821)(373)}{536 \times 10^{-3}} = 57.1 \text{ atm}$$

$$b) \quad \left(P + \frac{an^2}{V^2}\right)(V - nb) = nRT$$

$$\left(P + \frac{3.61}{(536 \times 10^{-3})^2}\right)(536 \times 10^{-3} - 0.0428) = 0.0821 \times 373$$

$$(P + 12.57)(0.4932) = 30.6233$$

$$P = \frac{30.6233}{0.4932} - 12.57$$

$$P = 49.52 \text{ atm}$$

6. Using Van der Waals equation, calculate the temperature of 20.0 mole of helium in a 10.0-liter cylinder at 120 atmosphere pressure.

[Data - Van der Waals constants for helium:  $a = 0.0341 \text{ L}^2 \text{ at mol}^{-2}$ ;  $b = 0.0237 \text{ L mol}^{-1}$ ]

$$P = 120 \text{ atm}$$

$$n = 20.0 \text{ mol}, V = 10.0 \text{ L}$$

$$(120 + 0.0341 \times (20.0/10.0)^2)(10.0 - 20.0 \times 0.0237) = 20.0 \times 0.0821 \times T$$

[Note the value of  $R = 0.0821$  because  $P$  is in atm and  $V$  in L]

$$(120 + 0.1364)(10.0 - 0.5) = 1.64 \times T$$

$$T = 696 \text{ K}$$

$$\left(P + \frac{an^2}{V^2}\right)(V - nb) = nRT$$

$$T = \frac{(120 + \frac{0.0341(20)^2}{10^2})(10 - 20 \times 0.0237)}{20 \times 0.0821} = 696 \text{ K}$$

$$F = \frac{9}{5}C + 32 = \frac{9}{5}(37) + 32 = 98.6$$

$$37 + 273.15 = 310.15$$

1. Convert 37°C to both Fahrenheit degrees and Kelvin.

$$F = \frac{9}{5}C + 32 = \frac{9}{5}(37) + 32 = 66.6 + 32 = 98.6^\circ \text{ F} \leftarrow \text{That's human body temp.}$$



2. Convert 80K to both Celsius and Fahrenheit degrees.

First convert to Celsius by subtracting 273.15 K:

$$T = 80 - 273.15 = -193.15^\circ \text{ C}$$

$$C = 80 - 273.15 = -193.15^\circ \text{ C}$$

$$F = \frac{9}{5}C + 32 = \frac{9}{5}(-193.15) + 32 = -347.7^\circ \text{ F}$$

$$\text{Then to Fahrenheit: } F = \frac{9}{5}C + 32 = \frac{9}{5}(-193.15) + 32 = -347.7^\circ \text{ F}$$

3. Calculate the difference between 97°F and 40°F in both Celsius degrees and Kelvin.

In Celsius degrees, these temperatures are

$$T_1 = \frac{9}{5}(F - 32) = \frac{9}{5}(97 - 32) = 37.22^\circ \text{ C}$$

$$T_2 = \frac{9}{5}(F - 32) = \frac{9}{5}(40 - 32) = 4.44^\circ \text{ C}$$

The difference is  $37.22 - 4.44 = 32.78^\circ \text{ C}$  or  $32.78 \text{ K}$

$$T_1(C) = \frac{5}{9}(F - 32)$$

$$T_1(C) = \frac{5}{9}(97 - 32) = 36.1$$

$$T_2(C) = \frac{5}{9}(40 - 32) = 4.44$$

$$\Delta T = 36.1 - 4.44 = 31.66^\circ \text{ C}$$

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$$\Delta T = 31.66 \text{ K}^\circ$$

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