

HW-1

Answer the following questions

- **Dimensional Analysis**

1. Which of the following equations are dimensionally correct?

(a) $v_f = v_i + ax$

(b) $y = (2 \text{ m})\cos(kx)$, where $k = 2 \text{ m}^{-1}$.

a) $v_f = v_i + ax$

$$\frac{L}{T} = \frac{L}{T} + \frac{L}{T^2} L$$

$$\frac{L}{T} = \frac{L}{T} + \frac{L^2}{T^2}$$

$$\text{LHS} \neq \text{RHS}$$

This equation is not dimensionally correct

b) $y = 2m \cos kx$

$$[L] = [L]$$

$$\text{LHS} = \text{RHS}$$

This equation is dimensionally

Correct

y :- مسانه $[L]$

m :- مسافه $[L]$

sin , cos ليس لها وحدة

2. The position of a particle moving under uniform acceleration is some function of time and the acceleration. Suppose we write this position $s = ka^m t^n$, where k is a dimensionless constant. Show by dimensional analysis that this expression is satisfied if $m=1$ and $n=2$. Can this analysis give the value of k ?

$$S = k a^m t^n$$

$$[L] = \left[\frac{L}{T^2} \right]^m [T]^n$$

$$[L] = [L]$$

$$n=2$$

$$m=1$$

لغى تحققت المعادلة عند وضع

$$LHS = RHS$$

$$S = \text{الموضع} = m = [L]$$

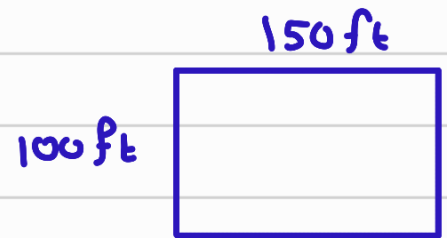
$$a = \text{تسارع} = m/s^2 = \left[\frac{L}{T^2} \right]$$

$$t = \text{زمن} = S = [T]$$

k is dimensionless constant
cannot be obtained by analysis

- Conversion of Units

3. A rectangular building lot is 100 ft by 150 ft . Determine the area of this lot in m^2 ? $1m = 3.281 ft$



تحويل الطول

$$L = \frac{150}{3.281} m$$

$$W = \frac{100}{3.281} m$$

$$Area = L W$$

$$Area = \frac{150}{3.281} \times \frac{100}{3.281} = 1393.4 m^2$$

$$= 1.3934 \times 10^3 m^2$$

$$= 1.39 \times 10^3 m^2$$